

zravnú radu enumeráciou

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$$P(b, j, m) = \sum_e \sum_a P(b, e, a, j, m)$$

$$= \sum_e \sum_a P(b) \cdot P(e) \cdot P(a|b, e) \cdot P(j|a) \cdot P(m|a)$$

$$= P(b) \cdot P(e) \cdot P(a|b, e) \cdot P(j|a) \cdot P(m|a) \\ + P(b) \cdot P(\neg e) \cdot P(a|b, \neg e) \cdot P(j|a) \cdot P(m|a) \\ + P(b) \cdot P(e) \cdot P(\neg a|b, e) \cdot P(j|\neg a) \cdot P(m|\neg a) \\ + P(b) \cdot P(\neg e) \cdot P(\neg a|b, \neg e) \cdot P(j|\neg a) \cdot P(m|\neg a)$$

$$= 0.001 \cdot \begin{array}{l} 0.002 \cdot 0.95 \cdot 0.9 \cdot 0.7 \quad 0.001197 \\ 0.998 \cdot 0.94 \cdot 0.9 \cdot 0.7 \quad 0.5910156 \\ 0.002 \cdot 0.05 \cdot 0.05 \cdot 0.01 \quad 0.00000005 \\ 0.998 \cdot 0.06 \cdot 0.05 \cdot 0.01 \quad 0.00002994 \\ \hline 0.59224259 \end{array}$$

$$= 0.001 \cdot [0.001197 + 0.5910156 + 0.00000005 + 0.00002994] \\ = \underline{\underline{0.00059224259}}$$

Za B = 7b (-b):

$$P(7b|j, m) = 0.999 \cdot \begin{array}{l} P(a|7b, e) \quad 0.0003654 \\ 0.002 \cdot 0.29 \cdot 0.63 \quad 0.00062874 \\ 0.998 \cdot 0.001 \cdot 0.63 \\ \hline P(a|7b, \neg e) \\ 0.002 \cdot P(\neg a|7b, e) \cdot 0.0005 \quad 0.00000071 \\ 0.71 \\ 0.998 \cdot 0.999 \cdot 0.0005 \quad 0.000498501 \\ \hline P(\neg a|7b, \neg e) \quad 0.001493351 \\ \hline 0.001491857649 \end{array}$$

zbroj = 0.002084100239

$$\alpha = \frac{1}{\dots} = 479.8233699.$$

$$\Rightarrow P(B|j, m) = \langle 0.284172, 0.715828 \rangle$$

Uočiti:  $\alpha = \frac{1}{P(j, m)}$ , tj. zbroj =  $P(j, m) = 0.002084\dots$

# Eliminacija

$$f_4(A) = \langle P(j|a) \quad P(j|\neg a) \rangle = \langle 0.90, 0.05 \rangle$$

$$f_5(A) = \langle P(m|a) \quad P(m|\neg a) \rangle = \langle 0.70, 0.01 \rangle$$

$$f_3(A, B, E) = \langle P(a|b, e), \dots, P(\neg a|\neg b, \neg e) \rangle$$

$$= \langle \begin{matrix} 0.95 & 0.05 & 0.94 & 0.06 & 0.29 & 0.71 & 0.001 & 0.999 \\ a & \neg a & a & \neg a & a & \neg a & a & \neg a \end{matrix} \rangle$$

Množenje ili združivanje faktora - srećom  $f_4, f_5$  onse samo o A

$f_3(A, B, E) \times f_4(A) \times f_5(A)$  ima ISTO 8 elem.

$$\langle 0.63, 0.0005 \rangle$$

a                       $\neg a$

NE  
formirah  
cijelu

Produkt:	A	B	E	produkt
	a	b	e	0.95
	a	b	$\neg e$	0.94
	a	$\neg b$	e	0.29
	a	$\neg b$	$\neg e$	0.001
	$\neg a$	b	e	0.05
	$\neg a$	b	$\neg e$	0.06
	$\neg a$	$\neg b$	e	0.71
	$\neg a$	$\neg b$	$\neg e$	0.999

} 0.63 =

} 0.0005 =

$$f_3(a, B, E) \cdot f_4(a) \cdot f_5(a) = 0.63 \cdot \langle 0.95 \quad 0.94 \quad 0.29 \quad 0.001 \rangle$$

$$f_3(\neg a, B, E) \cdot f_4(\neg a) \cdot f_5(\neg a) = 0.0005 \cdot \langle 0.05 \quad 0.06 \quad 0.71 \quad 0.999 \rangle$$

$$\text{prvi} = \langle 0.5985 \quad 0.5922 \quad 0.1827 \quad 0.00063 \rangle$$

$$\text{drugi} = \langle 0.00025 \quad 0.00003 \quad 0.000355 \quad 0.0004995 \rangle$$

zbroj

$$f_6(B, E) = \langle \begin{matrix} 0.598525 & 0.59223 & 0.183055 & 0.0011295 \\ b, e & b, \neg e & \neg b, e & \neg b, \neg e \end{matrix} \rangle$$

Ostaje izračunati

$$P(B | y, m) = \alpha \cdot f_1(B) \times \sum_e f_2(\epsilon) \times f_6(B, \epsilon) \quad 3$$

Eliminacija  $\epsilon =$  računamo  $f_2(\epsilon) = \langle 0.002 \quad 0.998 \rangle$

$$\begin{aligned} f_7(B) &= \sum_e f_2(\epsilon) \times f_6(B, \epsilon) \\ &= f_2(e) \times \underbrace{f_6(B, e)}_{\text{dulj 2}} + f_2(7e) \times \underbrace{f_6(B, 7e)}_{\text{dulj 2}} \end{aligned}$$

$$= 0.002 \cdot \langle 0.598 \ 525 \quad 0.183 \ 055 \rangle$$

$$+ 0.998 \cdot \langle 0.592 \ 23 \quad 0.001 \ 129 \ 5 \rangle$$

$$= \langle 0.001 \ 197 \ 05 \quad 0.000 \ 366 \ 11 \rangle$$

$$+ \langle 0.591 \ 045 \ 54 \quad 0.001 \ 127 \ 241 \rangle$$

$$f_7(B) = \langle 0.592 \ 242 \ 59 \quad 0.001 \ 493 \ 351 \rangle$$

$\quad \quad \quad b \quad \quad \quad 7b$

$$f_1(B) \times f_7(B), \text{ uz } f_1(B) = \langle 0.001 \ 0.999 \rangle$$

Računamo vektor/faktor  $f_8(B) = f_1(B) \times f_7(B)$

$$= \langle 0.001 \cdot 0.592 \ 242 \ 59 \quad 0.999 \cdot 0.001 \ 493 \ 351 \rangle$$

$$= \langle 0.000 \ 592 \ 242 \ 59 \quad 0.001 \ 491 \ 857 \ 649 \rangle$$

Rezultat  $P(B | y, m) = \alpha \cdot f_8(B)$   $\alpha$  da zbroj bude 1

Zbroj elem. u  $f_8(B) = 0.002 \ 084 \ 100 \ 239$

$$\alpha = \frac{1}{\text{zbroj}} = 479. \ 823 \ 369 \ 954 \dots$$

$$\Rightarrow \boxed{P(B | y, m) = \langle 0.284 \ 172 \dots, \ 0.715 \ 828 \rangle}$$

Račun drugim putem - prvo eliminiramo E, pa A

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1 Formula za račun - napisana u faktorima je

$$P(B|j,m) = \alpha \cdot f_1(B) \times \sum_a f_4(A) \times f_5(A) \times \sum_e f_2(\epsilon) \times f_3(A,B,\epsilon)$$

Prvo odsumiramo E iz produkta  $f_2(\epsilon) \times f_3(A,B,\epsilon)$  što daje faktor  $f_9(A,B)$

$$f_9(A,B) = \sum_e f_2(\epsilon) \times f_3(A,B,\epsilon)$$

$$= f_2(e) \cdot f_3(A,B,e) + f_2(7e) \cdot f_3(A,B,7e)$$

$$= 0.002 \cdot \begin{matrix} \langle 0.95 & 0.29 & 0.05 & 0.71 \rangle \\ a,b & a,7b & 7a,b & 7a,7b \end{matrix}$$

$$+ 0.998 \cdot \langle 0.94 & 0.001 & 0.06 & 0.999 \rangle$$

$$= \langle 0.0019 & 0.00058 & 0.0001 & 0.00142 \rangle$$

$$+ \langle 0.93812 & 0.000998 & 0.05988 & 0.997002 \rangle$$

$$f_9(A,B) = \begin{matrix} \langle 0.94002 & 0.001578 & 0.05998 & 0.998422 \rangle \\ a,b & a,7b & 7a,b & 7a,7b \end{matrix}$$

Sad odsumiramo A iz produkta  $f_4(A) \times f_5(A) \times f_9(A,B)$  što daje faktor  $f_{10}(B)$  (= ranijem  $f_7(B)$ )

$$f_{10}(B) = \sum_a f_4(A) \times f_5(A) \times f_9(A,B)$$

$$= 0.63$$

$$= f_4(a) \cdot f_5(a) \times \langle 0.94002 & 0.001578 \rangle \quad f_4(a) \cdot f_5(a) = 0.63$$

$$+ f_4(7a) \cdot f_5(7a) \times \langle 0.05998 & 0.998422 \rangle \quad f_4(7a) \cdot f_5(7a) = 0.0005$$

$$= \langle 0.5922126 & 0.00099414 \rangle$$

$$+ \langle 0.00002999 & 0.000499211 \rangle$$

$$f_{10}(B) = \langle 0.59224259 & 0.001493351 \rangle \quad \textcircled{W} = f_7(B)$$

Kraj računa  $P(B|j,m) = \alpha \cdot f_1(B) \times f_{10}(B)$  je ISTI kao malo prije!